Note

The relationship between induction temperature and time in the exothermic decomposition reaction of energetic materials

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According to our previous paper [l], the non-isothermal differential kinetic equation describing the fraction of material reacted with time is

$$
\frac{d\alpha}{dt} = \left\{ A \left[1 + \frac{E}{RT} \left(1 - \frac{T_0}{T} \right) \right] \exp \left(- \frac{E}{RT} \right) \right\} f(\alpha)
$$
\n(1)

where α , T, $f(\alpha)$, T₀, t, R, A and *E* have the usual meanings [1, 2]. Combining eqn. (1) and $T = T_0 + \varphi t$

$$
\frac{d\alpha}{f(\alpha)} = \frac{A}{\varphi} \left[1 + \frac{E}{RT} \left(1 - \frac{T_0}{T} \right) \right] \exp\left(- \frac{E}{RT} \right) dT \tag{2}
$$

where φ is the constant heating rate.

Integrating eqn. (2) between the initial temperature T_0 and the induction temperature T_{ind} , and the fraction of the material reacted between 0 and α_{ind} , yields

$$
\frac{1}{A} \int_0^{\alpha_{\text{ind}}} \frac{d\alpha}{f(\alpha)} = \frac{1}{\varphi} \int_{T_0}^{T_{\text{ind}}} \left[1 + \frac{E}{RT} \left(1 - \frac{T_0}{T} \right) \right] \exp\left(-\frac{E}{RT} \right) dT
$$
\n
$$
= \frac{1}{\varphi} \left(T_{\text{ind}} - T_0 \right) \exp\left(-\frac{E}{RT_{\text{ind}}} \right) \tag{3}
$$

For the case of an isothermal experiment at temperature T_{iso} , eqn. (1)

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can be written

$$
\frac{d\alpha}{dt} = Af(\alpha) \exp\left(-\frac{E}{RT_{iso}}\right)
$$
 (4)

and the variables can be separated to give

$$
\frac{1}{A}\frac{d\alpha}{f(\alpha)} = \exp\left(-\frac{E}{RT_{\text{iso}}}\right)dt\tag{5}
$$

Integrating eqn. (5) between 0 and the induction time t_{ind} , and the fraction of the material reacted between 0 and α'_{ind} , gives

$$
\frac{1}{A} \int_0^{\alpha'_{\text{ind}}} \frac{d\alpha}{f(\alpha)} = \exp\left(-\frac{E}{RT_{\text{iso}}}\right) \int_0^{t_{\text{ind}}} dt
$$

$$
= t_{\text{ind}} \exp\left(-\frac{E}{RT_{\text{iso}}}\right) \tag{6}
$$

Typical DSC curves defining these integration limits T_0 , T_{ind} , α_{ind} , t_0 , t_{ind} and α'_{ind} for a non-isothermal and an isothermal experiment are shown in Fig. 1.

The left-hand sides of eqns. (3) and (6) are equal if three assumptions are satisfied: (a) during the induction period, the value of α'_{ind} corresponding to the induction time t_{ind} in the isothermal experiment at temperature T_{iso} is equal to the value of α_{ind} corresponding to the induction temperature T_{ind} in the non-isothermal experiment at the constant heating rate φ ; (b) the most

Fig. 1. Typical isothermal and non-isothermal DSC curves of the exothermic decomposition reaction of ethylenediammonium salt of 3-nitro-1,2,4-triazol-5-one. Curve I, held at 490.15 K; curve II, heating rate of 5 K min⁻¹.

probable differential mechanism function, $f(\alpha)$ has the same form in both the isothermal and non-isothermal experiments; and (c) all variables, e.g. sample size and gas pressure, are the same for the isothermal and non-isothermal experiments. Thus the right-hand sides can be equated to give

$$
t_{\rm ind} = \frac{T_{\rm ind} - T_0}{\varphi} \exp\left[\frac{E}{R} \left(\frac{1}{T_{\rm iso}} - \frac{1}{T_{\rm ind}}\right)\right]
$$
 (7)

Taking logarithms on both sides of eqn. (7)

$$
\ln(t_{\rm ind})_i = B + \frac{E}{R} \left(\frac{1}{T_{\rm iso}} \right)_i \qquad i = 1, 2, ..., n
$$
 (8)

where

$$
B = \left[\ln \left(\frac{T_{\text{ind}} - T_0}{\varphi} \right) - \frac{E}{RT_{\text{ind}}} \right]
$$
 (9)

When In t_{ind} is plotted versus $1/T_{\text{so}}$ by the least-squares method, this gives the value of *E* from the slope.

Equations (7) or (8) relate the induction time t_{ind} of the thermal decomposition for an isothermal run at T_{iso} , to the induction temperature T_{ind} for a non-isothermal run at a heating rate of φ .

Rearranging both sides of eqn. (7) gives

$$
E = \frac{RT_{\text{iso}}T_{\text{ind}}}{T_{\text{ind}} - T_{\text{iso}}} \ln \left(\frac{\varphi t_{\text{ind}}}{T_{\text{ind}} - T_0} \right)
$$
(10)

By substituting the values of t_{ind} and T_{iso} obtained from an isothermal run, and the values of T_0 , T_{ind} and φ obtained from a non-isothermal run into eqn. (10), the corresponding value of E may be also determined.

Comparing eqn. (9) with the equation [3]

$$
\ln(t_{\rm ind})_i = C + \frac{E}{R} \left(\frac{1}{T_{\rm iso}}\right)_i \tag{11}
$$

where

$$
C = \ln[G(\alpha)] - \ln A \tag{12}
$$

derived under isothermal conditions yields

$$
\ln A = \ln \left[\frac{\varphi G(\alpha)}{T_{\text{ind}} - T_0} \right] + \frac{E}{RT_{\text{ind}}}
$$
\n(13)

Once the value of *E* has been calculated from eqn. (8) and the values of T_{ind} , T_0 and φ have been obtained from a non-isothermal run, and the value of the integral mechanism function $G(\alpha)$ has been obtained by the method

 X i. X i. Γ \sim Γ \sim Key: $T_{\text{R},\text{a}}$, temperature of isothermal run (K); t_{rad} , induction time (s); α_{rad} fraction of the material reacted during the inducing period for the ∞ point of the deviation from the baseline of the DSC curve (K); *A,* pre-exponential constant (s-l); *Elnd,non_,soj.* apparent energy obtained by Ozawa's y Key: T_{top} temperature of isothermal run (K); t_{mid} , induction time (s); α_{mid} fraction of the material reacted during the inducing period for the $\overline{}$ point of the deviation from the baseline of the DSC curve (K); A, pre-exponential constant (s⁻¹); $E_{\text{md}(\text{non--}88)}$, apparent energy obtained by Ozawa's non-isothermal run; E_{motoco}, apparent energy obtained from eqn. (8) under isothermal conditions (kJ mol⁻¹); r, linear correlation coefficient; φ , heating rate (K min \cdot); T_{max} , induction temperature (K); α'_{max} fraction of the material reacted during the induction period for the isothermal run; T_0 , the initial non-isothermal run; *Elndtlrol,* apparent energy obtained from eqn. (8) under isothermal conditions (kJ mol- '); r, linear correlation coefficient; cp, heating rate (K min '); *T_{rack}* induction temperature (K); α'_{rad} , fraction of the material reacted during the induction period for the isothermal run; *I*₀, the initial method $[4]$ under non-isothermal conditions (kJ mol⁻¹).

 $\overline{}$

 $T_{\rm T}$

TABLE

Į.

of logical choices [l], the corresponding value of pre-exponential constant may be obtained from eqn. (13).

To verify the reliability of eqn. (8), we measured the isothermal and non-isomermal DSC curves of the ethylenediammonium salt of 3-nitro-1,2,4-triazol-5-one, using the same experimental conditions of sample size, gas pressure, etc.; the results are shown in Table 1. Because $\alpha'_{\text{ind}} \approx \alpha_{\text{ind}}$, $E_{\text{ind}(iso)} \approx E_{\text{ind}(non\text{-}iso)}$ and $[\ln(T_{\text{ind}} - T_0/\varphi) - E_{\text{ind}(iso)}/RT_{\text{ind}}] \approx [\ln G(\alpha) - \ln A]$ (i.e. $B \approx C$) (see Table 1), we conclude that our eqn. (7) is tenable.

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